WBJEE - 2020						
Answer Keys by Aakash Institute, Kolkata Centre						
	/ land	MATHEMAT	ICS			
Q.No.	Ŷ	+	0			
01	A	D	*	D		
02	A	B	B	B		
03	D	A	C	D		
05	В	А	С	В		
06	D	В	C	С		
07	C	C	B	D		
09	C	D	A	D		
10	В	*	A	В		
11	C	B	С	B		
12	A	C	B	A		
14	A	C	D	В		
15	A	С	C	D		
16	B	A	C	C		
18	D	A	В	*		
19	B	A	C	В		
20	A	С	A	С		
21	B	D	A	C		
22	C	D	A	C		
24	A	C	B	A		
25	D	С	С	В		
26	D	С	D	A		
27	B	В	A	A		
29	D	A	В	D		
30	В	А	D	В		
31	C	A	C	D		
32	D	B	D	C C		
34	D	C	D	C		
35	В	D	В	В		
36	В	В	В	C		
37	A	B	B	A		
39	В	D	C	A		
40	D	С	В	A		
41	С	A	D	В		
42	*	D	B	D		
44	В	B	B	В		
45	С	В	A	A		
46	C	D	A	В		
47	C C	СВ	D	C C		
49	A	В	C	A		
50	В	D	D	D		
51	С	С	B	D		
52	С В	СВ	C B	C B		
54	C	B	В	c		
55	С	В	С	В		
56	A	С	C	C		
57	ם ח	C. B	A	B		
59	B	C	D	C C		
60	С	С	D	С		
61	С	A	В	C C		
62	С В	ט ם	C C	C C		
64	В	В	В	Ă		
65	В	С	С	D		
66	В	D	C	C,D		
68	A,D A C	A C	A,C R	A,B D		
69	B	A,C	A,D	A		
70	C,D	В	A,C	С		
71	A,B	A,D	В	A,C		
72	D ۵	A,C R	C,D	B A D		
74	C	C,D	D	A,C		
75	A.C	A,B	A	В		

\* No correct option



Mathematics





**ANSWERS & HINT** 

## for

# WBJEE - 2020 SUB : MATHEMATICS

## CATEGORY - I (Q1 to Q50)

Carry 1 mark each and only one option is correct. In case of incorrect answer or any combination of more than one answer, <sup>1</sup>/<sub>4</sub> mark will be deducted.

1. Let  $\cos^{-1}\left(\frac{y}{b}\right) = \log\left(\frac{x}{n}\right)^n$ . Then

(A)  $x^2y_2 + xy_1 + n^2y = 0$  (B)  $xy_2 - xy_1 + 2n^2y = 0$  (C)  $x^2y_2 + 3xy_1 - n^2y = 0$  (D)  $xy_2 + 5xy_1 - 3y = 0$ Ans: (A)

**Hint**: 
$$\cos^{-1}\left(\frac{y}{b}\right) = \log\left(\frac{x}{n}\right)^n = n \times \log\left(\frac{x}{n}\right)$$

$$\Rightarrow -\frac{1}{\sqrt{b^2 - y^2}}.y_1 = \frac{n}{x}$$

$$\Rightarrow x^2 y_1^2 = n^2(b^2 - y^2) \Rightarrow x^2 y_2 + x y_1 + n^2 y = 0$$

2. Let 
$$\phi(x) = f(x) + f(1-x)$$
 and  $f''(x) < 0$  in [0, 1], then

(A)  $\phi$  is monotonic increasing in  $\left[0, \frac{1}{2}\right]$  and monotonic decrasing in  $\left[\frac{1}{2}, 1\right]$ 

 $\varphi$  is monotonic increasing in  $\left[\frac{1}{2}, 1\right]$  and monotonic decrasing in  $\left[0, \frac{1}{2}\right]$ 

(C)  $\phi$  is neither increasing nor decreasing in any sub interval of [0, 1]

(D) 
$$\phi$$
 is increasing [0, 1]

Ans:(A)

(B)

**Hint** : 
$$\phi'(x) = f'(x) - f'(1-x)$$

 $f'(x) - f'(1-x) \ge 0$  (for monotonic increasing)

 $f'(x) \ \ge \ f'(1-x), x \ \le \ 1-x \ ( \cdots \ f'(x) \text{ is decreasing})$ 

$$x \le \frac{1}{2} \Rightarrow \phi(x)$$
 is monotonic increasing in  $\begin{bmatrix} 0, \frac{1}{2} \end{bmatrix}$  and monotonic decreasing in  $\begin{bmatrix} \frac{1}{2}, 1 \end{bmatrix}$ 

3. 
$$\int \frac{f(x)\varphi(x) + \varphi(x)^{1}(x)}{f(x)\varphi(x) + \varphi(x)^{1}(x)} dx =$$
(A)  $\sin^{-1}\sqrt{\frac{f(x)}{\varphi(x)}} + c$  (B)  $\cos^{-1}\sqrt{(f(x))^{2} - (\varphi(x))^{2}} + c$ 
(C)  $\sqrt{2}\tan^{-1}\sqrt{\frac{f(x)\varphi(x) - 1}{2}} + c$  (D)  $\sqrt{2}\tan^{-1}\sqrt{\frac{f(x)\varphi(x) - 1}{2}} + c$ 
Ans: (C)
Hint: Let  $f(x) \phi(x) = t$ 

$$\int \frac{1}{(t: 1)\sqrt{t-1}}$$
Let  $t-1 = p^{2}$ ,  $dt = 2p dp$ 

$$= \int \frac{2dp}{p^{2} + 2} = \sqrt{2}\tan^{-1}\sqrt{\frac{f(x)\varphi(x) - 1}{2}} + c$$
4. The value of  $\sum_{n=1}^{\infty} \sum_{j=1}^{\infty} \sin^{nj}x dx + \sum_{n=1}^{\infty} \sum_{j=1}^{\infty} \sin^{nj}x dx$  is equal to
(A) 27 (B) 54 (C)  $-54$  (D) 0
Ans: (D)
Hint:  $\sum_{n=1}^{\infty} \sum_{j=1}^{\infty} \sin^{nj}x dx + \sum_{n=1}^{\infty} \sum_{j=1}^{\infty} \sin^{nj}x dx$ 

$$= 0$$
5.  $\sum_{n=1}^{\frac{1}{2}} \left[ x^{n-1} dx + \sum_{j=1}^{\infty} \sum_{j=1}^{\infty} \sin^{nj}x dx$ 

$$= 0$$
5.  $\int_{0}^{\frac{1}{2}} \left[ x^{n-1} dx + \sum_{j=1}^{\infty} \sum_{j=1}^{\infty} \sin^{nj}x dx$ 

$$= 0$$
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$$= 0$$
5.  $\int_{0}^{\frac{1}{2}} \left[ x^{n-1} dx + \sum_{j=1}^{\infty} \sum_{j=1}^{\infty} \sin^{nj}x dx$ 

$$= 0$$
6. If the tangent to the curve  $y^{2} = x^{2} at (m^{2}, m^{2}) is also a normal to the curve at (M^{2}, M^{2}), then the value of mM is
(A)  $-\frac{1}{9}$  (B)  $-\frac{2}{9}$  (C)  $-\frac{1}{3}$  (D)  $-\frac{4}{9}$ 
Ans: (D)
Hint:  $2y_{N} = 3x^{2}$ 
 $y_{N} = \frac{3x^{2}}{2y} \Rightarrow (x_{N})_{nd', nd'} = \frac{3}{3M}$ ,  $mM = -\frac{4}{9}$$ 

If  $x^2 + y^2 = a^2$ , then  $\int_a^a \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx =$ 7. (C)  $\frac{1}{2}\pi a$ (D)  $\frac{1}{4}\pi a$ (A) 2πa (B) πa Ans:(C) Hint:  $y_1 = -\frac{x}{v}$  $\int_{a}^{a} \sqrt{1 + \frac{x^{2}}{v^{2}}} dx = a \int_{a}^{a} \frac{1}{v} dx = a \int_{a}^{a} \frac{dx}{\sqrt{a^{2} - x^{2}}}$  $=a\left[\sin^{-1}\left(\frac{x}{a}\right)\right]_{a}^{a}=a\pi/2$ Let f, be a continuous function in [0, 1], then  $\lim_{n\to\infty}\sum_{j=0}^{n}\frac{1}{n}f(\frac{j}{n})$  is 8. (A)  $\frac{1}{2}\int_{-1}^{\frac{1}{2}}f(x)dx$ (B)  $\int_{\frac{1}{2}}^{f(x)dx}$ (C)  $\int_{0}^{1} f(x) dx$ (D)  $\int_{-\infty}^{2} f(x) dx$ Ans:(C) Hint :  $\int_{1}^{1} f(x) dx$ Let f be a differentiable function with  $\lim_{x\to\infty} f(x) = 0$ . If y' + yf'(x) - f(x)f'(x) = 0,  $\lim_{x\to\infty} y(x) = 0$ , then  $\left( \text{ where } y' = \frac{dy}{dx} \right)$ 9. (A)  $y + 1 = e^{f(x)} + f(x)$ (B)  $y - 1 = e^{f(x)} + f(x)$ (C)  $y + 1 = e^{-f(x)} + f(x)$  (D)  $y - 1 = e^{-(f)x} + f(x)$ Ans:(C) Hint:  $\frac{dy}{dx} + f'(x)y = f'(x)f(x)$  $\Rightarrow y \times e^{f(x)} = \int f'(x)f(x)e^{f(x)}dx$  $\Rightarrow y \times e^{f(x)} = e^{f(x)}(f(x) - 1) + c$  [Putting f(x) = 0; y = 0, c = 1]  $\Rightarrow$  y × e<sup>f(x)</sup> = e<sup>f(x)</sup>(f(x) - 1) + 1  $\Rightarrow$  y = f(x) - 1 + e<sup>-f(x)</sup>  $\Rightarrow$  y + 1 = e<sup>-f(x)</sup> + f(x) 10. If  $x \sin\left(\frac{y}{x}\right) dy = \left[y \sin\left(\frac{y}{x}\right) - x\right] dx$ , x > 0 and  $y(1) = \frac{\pi}{2}$  then the value of  $\cos\left(\frac{y}{x}\right)$  is (A) 1 (C) e (B) logx (D) 0 Ans:(B) **Hint**:  $\sin v \left( v + x \cdot \frac{dv}{dx} \right) = v \sin v - 1$ 

 $\Rightarrow$  x sin v.  $\frac{dv}{dx} = -1$  $\Rightarrow \int \sin v \, dv = -\int \frac{dx}{v}$  $\Rightarrow$  -cosv = - logx + c at x = 1 ; y =  $\frac{\pi}{2}$  ; c = 0  $\cos\left(\frac{y}{x}\right) = \log x$ 11. Let  $f(x) = 1 - \sqrt{x^2}$  where the square root is to be taken positive, then (A) f has no extrema at x = 0(B) f has minima at x = 0(C) f has maxima at x = 0 (D) f' exists at 0 Ans:(C) **Hint** : f(x) = 1 - |x|, f has maxima at x = 012. If the function  $f(x) = 2x^3 - 9ax^2 + 12a^2x + 1[a > 0]$  attains its maximum and minimum at p and q respectively such that  $p^2 = q$ , then a is equal to (B)  $\frac{1}{2}$ (A) 2 (C) (D) 3 Ans:(A) Hint :  $f'(x) = 6x^2 - 18ax + 12a^2 \Rightarrow f''(x) = 12x - 18a \Rightarrow f'(x) = 0 \Rightarrow x = a, 2a$ f''(a) < 0; p = a (maximum) f''(2a) > 0; q = 2a (minimum)  $a^2 = 2a$ ; a(a - 2) = 0, a = 213. If a and b are arbitrary positive real numbers, then the least possible value of  $\frac{6a}{5h} + \frac{10b}{3a}$  is (C)  $\frac{10}{3}$ (D)  $\frac{68}{15}$ (B)  $\frac{6}{5}$ (A) 4 Ans:(A) **Hint :**  $\frac{6a}{5b} + \frac{10b}{3a} \ge 2\sqrt{\frac{6a}{5b} \times \frac{10b}{3a}}$ ,  $\frac{6a}{5b} + \frac{10b}{3a} \ge 2 \times 2 \ge 4$ 14. If  $2\log(x+1) - \log(x^2-1) = \log 2$ , then x =(C) only -1 (A) only 3 (B) -1 and 3 (D) 1 and 3 Ans:(A) Hint:  $\log \left\{ \frac{(x+1)^2}{x^2-1} \right\} = \log 2 \implies (x+1)^2 = 2(x^2-1) \implies x^2-2x-3=0 \implies (x-3)(x+1)=0$ x = 3;  $x \neq -1$ 

Mathematics

15.	The number of complex n	umbers p such that $ p  = 1$ and	limag	jinary part of p⁴ is 0, is		
	(A) 4	(B) 2	(C)	8	(D)	infinitely many
	Ans : (A)					
	<b>Hint :</b> Let $p = x + iy$ , $p^2 =$	$= (x^2 - y^2) + 2ixy, p^4 = (x^2 - y^2)$	<sup>2</sup> – 4)	$(x^2y^2 + 4ixy (x^2 - y^2))$		
	Now, $xy(x^2 - y^2) = 0$ , x	$=\pm y \Rightarrow y^2 = \frac{1}{2} \Rightarrow y = \pm \frac{1}{\sqrt{2}}$				
	Four complex numbers .					
16.	The equation $z\overline{z} + (2-3i)z$	$+(2+3i)\overline{z}+4=0$ represents a c	ircle	of radius		
	(A) 2 unit	(B) 3 unit	(C)	4 unit	(D)	6 unit
	Ans:(B)					
	Hint : Centre and radius of	of $z\overline{z} + \overline{a}z + a\overline{z} + b = 0$ are –a and	d √∣a	$\overline{ ^2 - b}$ : radius = $\sqrt{13 - 4}$	= 3	
17.	The expression ax <sup>2</sup> + bx +	c (a, b and c are real) has the	e sam	e sign as that of a for al	l x if	
	(A) $b^2 - 4ac > 0$		(B)	$b^2 - 4ac \neq 0$		
	(C) $b^2 - 4ac \le 0$		(D)	b and c have the same	e sigr	as that of a
	Ans : (C)					
	<b>Hint :</b> C-I: If $a > 0$ , $ax^2 +$	$bx + c > 0, b^2 - 4ac < 0, C-1$	l: If a	$a \le 0, ax^2 + bx + c \le 0,$	D ≤ 0	)
18.	In a 12 storied building, 3 many ways can they do se	persons enter a lift cabin. It is o if the lift does not stop at the	know seco	n that they will leave the nd floor ?	e lift a	at different floors. In how
	(A) 36	(B) 120	(C)	240	(D)	720
	Ans : (D)					
	Hint : Total no. of ways =	$10_{p_3} = 720$ (except the floor the	ey ent	er and second floor)		
19.	If the total number of m-e containing $a_4$ , then n is	lement subsets of the set A =	{a₁, a	$_{2}, \dots, a_{n}$ is k times the r	umb	er of m element subsets
	(A) (m – 1)k	(B) mk	(C)	(m + 1)k	(D)	(m + 2)k
	Ans : (B)					
	<b>Hint :</b> $n_{c_m} = k \cdot {}^{n-1}c_{m-1} \Longrightarrow n$	= mk				
20.	Let $I(n) = n^n$ , $J(n) = 1.3.5$ .	$(2n - 1)$ for all $(n > 1)$ , $n \in I$	N, the	n		
	(A) $I(n) > J(n)$	(B) $I(n) < J(n)$	(C)	I(n) = J(n)	(D)	$I(n) = \frac{1}{2}J(n)$
	Ans : (A)					
	$\textbf{Hint}: AM \geq GM$					
	$\frac{1 + 3 + 5 + 7 + \ldots + (2n - 1)}{n} > 0$	$(J(n))^{\frac{1}{n}},  \frac{n^2}{n} > (J(n))^{\frac{1}{n}},  n^n > J_n$	(n),	I(n) > J(n)		
21.	If c <sub>o</sub> , c <sub>o</sub> , c <sub>o</sub> , c <sub>or</sub> are the B	sinomial co-efficients in the expa	ansior	$1 \text{ of } (1 + x)^{15}$ , then the value	ie of -	$\frac{c_1}{c_1} + 2\frac{c_2}{c_2} + 3\frac{c_3}{c_3} + \dots + 15\frac{c_{15}}{c_{15}}$
	is					$c_0 c_1 c_2 c_{14}$
	(A) 1240	(B) 120	(C)	124	(D)	140
	Ans : (B)	· /			. /	
	<b>Hint</b> : $S_n = \sum_{r=1}^{15} r \frac{{}^{15}C_r}{{}^{15}C_{r-1}} = \sum_{r=1}^{15} (r)^{15}C_{r-1}$	$(15-r+1) = 16 \times 15 - \frac{15 \times 16}{2} = 1$	20			

22. Let  $A = \begin{pmatrix} 3-t & 1 & 0 \\ -1 & 3-t & 1 \\ 0 & -1 & 0 \end{pmatrix}$  and det A = 5, then (A) t = 1 (B) t = 2 (C) t = −1 (D) t = -2Ans:(D) 3-t 1 0 **Hint :**  $|A| = \begin{vmatrix} -1 & 3-t & 1 \\ 0 & -1 & 0 \end{vmatrix} = 3 - t = 5, t = -2$ (12 24 5) 23. Let  $A = \begin{bmatrix} x & 6 & 2 \\ -1 & -2 & 3 \end{bmatrix}$ . The value of x for which the matrix A is not invertible is (C) 3 (A) 6 (B) 12 (D) 2 Ans:(C) **Hint** : If matrix is not invertible  $\Rightarrow |A| = 0$  $\therefore |\mathsf{A}| = \begin{vmatrix} 12 & 24 & 5 \\ x & 6 & 2 \end{vmatrix} = 0 \Longrightarrow x = 3$ -1 -2 3 24. Let  $A = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$  be a 2 x 2 real matrix with det A = 1. If the equation det  $(A - \lambda I_2) = 0$  has imaginary roots ( $I_2$  be the Identity matrix of order 2), then (C)  $(a + d)^2 > 4$  (D)  $(a + d)^2 = 16$ (A)  $(a + d)^2 < 4$ (B)  $(a + d)^2 = 4$ Ans:(A) **Hint :** |A| = 0 : ad -bc = 1 $|A - \lambda I_2| = 0$  $\begin{vmatrix} a - \lambda & b \\ c & d - \lambda \end{vmatrix} = 0$  $\therefore$  ad - (a + d) $\lambda$  +  $\lambda^2$  - bc = 0  $\lambda^2 - (a + d)\lambda + 1 = 0$ :.  $(a + d)^2 < 4$  $a^2$  bc  $c^2 + ac$ 25. If  $\begin{vmatrix} a^2 + ab \\ b^2 \end{vmatrix}$  ca  $\begin{vmatrix} = ka^2b^2c^2 \end{vmatrix}$ , then k = ab  $b^2 + bc$   $c^2$ (A) 2 (B) –2 (C) –4 (D) 4 Ans:(D) Hint:  $\begin{vmatrix} a^2 & bc & c^2 + ac \\ a^2 + ab & b^2 & ca \\ ab & b^2 + bc & c^2 \end{vmatrix} = (abc) \begin{vmatrix} a & c & a+c \\ a+b & b & a \\ b & b+c & c \end{vmatrix}$ ab  $b^2 + bc$   $c^2$ opening through R  $-1 = 4a^2b^2c^2$ 

26. If  $f: S \to \mathbb{R}$  where S is the set of all non-singular matrices of order 2 over  $\mathbb{R}$  and  $f\begin{bmatrix} a & b \\ c & d \end{bmatrix} = ad - bc$ , then (A) f is bijective mapping (B) f is one-one but not onto (C) f is onto but not one-one (D) f is neither one-one nor onto Ans:(D) **Hint**:  $f\begin{bmatrix} 2 & 0\\ 0 & 2 \end{bmatrix} = 4 = f\begin{bmatrix} 4 & 0\\ 0 & 1 \end{bmatrix}$  $\Rightarrow$  not one-one As  $0 \in \mathbb{R}$  but S does not contain any singular matrix so, f is not onto 27. Le the relation  $\rho$  be defined on  $\mathbb{R}$  by a  $\rho$  b holds if and only if a – b is zero or irrational, then (A) ρ is equivalence relation (B) ρ is reflexive & symmetric but is not transitive (C)  $\rho$  is reflexive and transitive but is not symmetric (D)  $\rho$  is reflexive only Ans:(B) **Hint** : If a - b = 0 then b - a = 0, if a – b is irrational then b – a is irrational  $\therefore$  a  $\rho$  b  $\Rightarrow$  b  $\rho$  a  $\Rightarrow$  symmetric  $\forall a \in \mathbb{R}$ , a - a = 0 a  $\rho a \Rightarrow$  reflexive If a = 2, b =  $\sqrt{2}$ , c = 3, then a  $\rho$  b, b  $\rho$  c but a  $\rho$  c is not true  $\Rightarrow$  not transitive 28. The unit vector in ZOX plane, making angles 45° and 60° respectively with  $\vec{\alpha} = 2\hat{i} + 2\hat{j} - \hat{k}$  and  $\vec{\beta} = \hat{j} - \hat{k}$  is (C)  $\frac{1}{\sqrt{2}}\hat{i} - \frac{1}{\sqrt{2}}\hat{j}$ (A)  $\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j}$ (B)  $\frac{1}{\sqrt{2}}\hat{i} - \frac{1}{\sqrt{2}}\hat{k}$ (D)  $\frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{k}$ Ans:(B) **Hint** : Let the vector be  $\vec{r} = x\hat{i} + z\hat{k} \Rightarrow |\vec{r}| = 1$  $\vec{r} \cdot \vec{\alpha} = |\vec{r}| |\vec{\alpha}| \cos 45^\circ$  $\therefore 2x - z = \frac{3}{\sqrt{2}}$  $\vec{r} \cdot \vec{\beta} = |\vec{r}| |\vec{\beta}| \cos 60^\circ$  $z = -\frac{1}{\sqrt{2}}$  $\therefore \mathbf{x} = \frac{1}{\sqrt{2}}$  $\therefore$   $\vec{r} = \frac{1}{\sqrt{2}}\hat{i} - \frac{1}{\sqrt{2}}\hat{k}$ 29. Four persons A, B, C and D throw an unbiased die, turn by turn, in succession till one gets an even number and win the game. What is the probability that A wins if A begins ? (D)  $\frac{8}{15}$ (C)  $\frac{7}{12}$ (A)  $\frac{1}{4}$ (B)  $\frac{1}{2}$ Ans:(D)

**Hint**: P(A win) =  $(\frac{1}{2}) + (\frac{1}{2})^4 (\frac{1}{2}) + (\frac{1}{2})^8 (\frac{1}{2}) + \cdots$  $= \frac{\frac{1}{2}}{1 - \left(\frac{1}{2}\right)^4} = \frac{\frac{1}{2}}{\frac{15}{16}} = \frac{8}{15}$ 30. A rifleman is firing at a distant target and has only 10% chance of hitting it. The least number of rounds he must fire to have more than 50% chance of hitting it at least once, is (D) 11 (A) 5 (B) 7 (C) 9 Ans:(B) **Hint** : P(hitting a target) =  $\frac{1}{10}$  $\therefore$  P(not hitting a target) =  $\frac{9}{10}$ : Let number of trials = n So, P(hitting at least once) = 1 - P (missing all) =  $1 - \left(\frac{9}{10}\right)^n \ge \frac{1}{2}$  $\Rightarrow$  (0.9)<sup>n</sup>  $\leq$  0.5  $(0.9)^6 = 0.531441, (0.9)^7 = 0.4782969 \implies n = 7$ 31.  $\cos(2x + 7) = a(2 - \sin x) \cosh a x$  real solution for (A) all real values of a (B)  $a \in [2, 6]$ (C)  $a \in [-\infty, 2] \setminus \{0\}$  (D)  $a \in (0, \infty)$ Ans:(C) Hint : By sandwich theorem 32. The differential equation of the family of curves  $y = e^x (A \cos x + B \sin x)$  where A, B are arbitrary constants is (A)  $\frac{d^2y}{dx^2} - 9x = 13$  (B)  $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + 2y = 0$  (C)  $\frac{d^2y}{dx^2} + 3y = 4$  (D)  $\left(\frac{dy}{dx}\right)^2 + \frac{dy}{dx} - xy = 0$ Ans:(B) **Hint**:  $y = e^x (A \cos x + B \sin x)$ Differentiating w.r.t. x: $y' = y + e^x (-Asin x + B cos x)$ Differentiating w.r.t. x once again: $y'' = y' + (y' - y) + e^{x} (-A \cos x - B \sin x)$  $= 2y' - y - y \implies y'' - 2y' + 2y = 0$ 33. The equation  $r\cos\left(\theta - \frac{\pi}{3}\right) = 2$  represents (A) a circle (B) a parabola (C) an ellipse (D) a straight line Ans:(D) **Hint**:  $\operatorname{rcos}\left(\theta - \frac{\pi}{3}\right) = 2$   $\Rightarrow \operatorname{rcos} \theta \times \frac{1}{2} + \operatorname{rsin} \theta \times \frac{\sqrt{3}}{2} = 2 \Rightarrow x + \sqrt{3}y = 4 \text{ (}x = \operatorname{rcos} \theta, y = \operatorname{rsin} \theta\text{)}$ .: a straight line

## WBJEE - 2020 (Answers & Hint) Mathematics 34. The locus of the centre of the circles which touch both the circles $x^2 + y^2 = a^2$ and $x^2 + y^2 = 4ax$ externally is (A) a circle an ellipse (B) a parabola (C) (D) a hyperbola Ans:(D) **Hint**: Let, centre $\equiv$ (h, k) and radius = r for the variable circle So, using $C_1C_2 = r_1 + r_2$ for both cases we have: $h^{2} + k^{2} = (r + a)^{2} \rightarrow (1)$ and $(h - 2a)^{2} + k^{2} = (r + 2a)^{2} \rightarrow (2)$ Eq. (2) – Eq. (1), gives : $r = \frac{a - 4h}{2} \rightarrow (3)$ Substitute (3) in (1) to get: $12h^2 - 4k^2 - 24ah + 9a^2 = 0$ $\therefore$ locus : $12x^2 - 4y^2 - 24ax + 9a^2 = 0$ i.e. a hyperbola 35. Let each of the equations $x^2 + 2xy + ay^2 = 0$ & $ax^2 + 2xy + y^2 = 0$ represent two straight lines passing through the origin. If they have a common line, then the other two lines are given by (A) x - y = 0, x - 3y = 0 (B) x + 3y = 0, 3x + y = 0 (C) 3x + y = 0, 3x - y = 0 (D) (3x - 2y) = 0, x + y = 0Ans:(B) $\left(\frac{x}{y}\right)^2 + 2\left(\frac{x}{y}\right) + a = 0$ & $a\left(\frac{x}{y}\right)^2 + 2\left(\frac{x}{y}\right) + 1 = 0$ have exactly one root in common (taking $\frac{x}{y}$ as a single Hint: variable). By, $(a_1b_2 - a_2b_1)(b_1c_2 - b_2c_1) = (a_1c_2 - a_2c_1)^2$ We get : $\Rightarrow$ a = 1 or -3a cannot be 1 Taking a = -3, roots of 1st equation : 1, -3 and 2nd equation : 1, -So other lines : $\frac{x}{v} = -3$ and $\frac{x}{v} = -\frac{1}{3}$ 36. A straight line through the origin O meets the parallel lines 4x + 2y = 9 and 2x + y + 6 = 0 at P and Q respectively. The point O divides the segment PQ in the ratio (A) 1:2 (B) 3:4 (C) 2:1 (D) 4:3 Ans:(B) Hint : $\triangle OPM \sim \triangle OQN$ $\Rightarrow \frac{OP}{OQ} = \frac{OM}{ON} = \Rightarrow \frac{\frac{9}{2}}{\frac{12}{2}} = \frac{3}{4}$

Mathematics









 $b = \frac{1}{2}; a = \frac{1}{4}; c = \frac{1}{4}$ 54. If the vectors  $\vec{\alpha} = \hat{i} + a\hat{j} + a^2\hat{k}$ ,  $\vec{\beta} = \hat{i} + b\hat{j} + b^2\hat{k}$ , and  $\vec{\gamma} = \hat{i} + c\hat{j} + c^2\hat{k}$  are three non-coplanar vectors and  $\begin{vmatrix} a & a^2 & 1 + a^3 \\ b & b^2 & 1 + b^3 \\ c & c^2 & 1 + c^3 \end{vmatrix} = 0$ , then the value of abc is (A) 1 (B) 0 (D) 2 (C) -1 Ans:(C) Hint:  $\begin{vmatrix} a & a^2 & 1 \\ b & b^2 & 1 \\ c & c^2 & 1 \end{vmatrix} (1 + abc) = 0$ abc = -1 [ $: \vec{\alpha}, \vec{\beta}, \vec{\gamma}$  are non-coplanar vector] 55. Let  $z_1$  and  $z_2$  be two imaginary roots of  $z^2 + pz + q = 0$ , where p and q are real. The points  $z_1$ ,  $z_2$  and origin form an equilateral triangle if (A)  $p^2 > 3q$ (B)  $p^2 < 3q$ (C)  $p^2 = 3q$ (D)  $p^2 = q$ Ans:(C) **Hint**:  $O^2 + Z_1^2 + Z_2^2 = Z_1Z_2$  $\Rightarrow$  Z<sub>1</sub><sup>2</sup> + Z<sub>2</sub><sup>2</sup> = Z<sub>1</sub>Z<sub>2</sub>  $\Rightarrow$  ( $z_1 + z_2$ )<sup>2</sup> =  $3z_1z_2$  $\Rightarrow p^2 = 3q$ 56. If  $P(x) = ax^2 + bx + c$  and  $Q(x) = -ax^2 + dx + c$ , where  $ac \neq 0$  [a, b, c, d are all real], then P(x).Q(x) = 0 has (A) at least two real roots (B) two real roots (C) four real roots (D) no real root Ans:(A) **Hint**: If  $P(x) = ax^2 + bx + c$ ,  $Q(x) = -ax^2 + dx + c$  $D_1 = b^2 - 4ac$  $D_{2} = d^{2} + 4ac$  $\Rightarrow$  D<sub>1</sub> + D<sub>2</sub> > 0 Atleast two real roots. 57. Let  $A = \{x \in \mathbb{R} : -1 \le x \le 1\}$  & f : A  $\rightarrow$  A be a mapping defined by f(x) = x|x|. Then f is (A) injective but not surjective (B) surjective but not injective (C) neither injective nor surjective (D) bijective Ans:(D) Hint:  $f(x) = x|x| = \begin{cases} -x^2 & x \in [-1, 0] \\ x^2 & x \in [0, 1] \end{cases}$  $\downarrow$ f(x) is bijective

58.	. Let $f(x) = \sqrt{x^2 - 3x + 2}$ and $g(x) = \sqrt{x}$ be two given functions. If S be the domain of $f \circ g$ and T be the domain of $g \circ f$ , then							
	(A) S = T	(B) §	$S \cap T = \varphi$	(C)	$S \cap T$ is a singleton	(D)	$S \cap T$ is an interval	
	Ans : (D)							
	<b>Hint</b> : $f(x) = \sqrt{(x-1)^2}$	$\overline{(x-2)}$ , g(x) =	$=\sqrt{x}$					
	$f(g(x)) = \sqrt{\sqrt{x}}$	$\overline{(x-1)}(\sqrt{x}-2)$						
	$S = \{x : x \in [0, $	,1]∪[4,∞)}						
	$g(f(x)) = \sqrt{\sqrt{x}}$	$\overline{(x-1)(x-2)}$						
	$T = \{x : x \in (\neg \neg$	∞, 1]∪[2,∞)}						
59.	Let $\rho_{_1}~~\text{and}~\rho_{_2}~\text{be two}$	equivalence	relations defined on a r	non-v	oid set S. Then			
	(A) both $\rho_1 \cap \rho_2$ and	d $\rho_1 \cup \rho_2$ are (	equivalence relations					
	(B) $\rho_1 \cap \rho_2$ is equiva	alence relatio	on but $\rho_1 \cup \rho_2$ is not so.					
	(C) $\rho_1 \cup \rho_2$ is equiv	alence relati	ion but $\rho_1 \cap \rho_2$ is not so	C				
	(D) neither $\rho_1 \cap \rho_2$ r	nor $\rho_1 \cup \rho_2$ is	equivalence relation.					
	Ans : (B)							
	Hint : Union of two tra	ansitive may	or may not be transitiv	е				
	x	$x^{2}$ $y^{2}$						
60.	Consider the curve $\frac{\pi}{a}$	$\frac{x}{a^2} + \frac{y}{b^2} = 1.$ Th	he portion of the tanger	nt at a	ny point of the curve int	ercep	ted between the point of	
60.	Consider the curve $\frac{2}{a}$ contact and the direc	$\frac{x}{a^2} + \frac{y}{b^2} = 1$ . The strict subtends	he portion of the tanger s at the corresponding f	nt at a focus	ny point of the curve int an angle of	ercep	ted between the point of	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direc (A) $\frac{\pi}{4}$	$\frac{x}{a^2} + \frac{y}{b^2} = 1.$ The strict subtends (B) $\frac{z}{c}$	he portion of the tanger s at the corresponding f $\frac{\pi}{3}$	nt at a focus (C)	ny point of the curve int an angle of $\frac{\pi}{2}$	ercep (D)	ted between the point of $\frac{\pi}{6}$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direc (A) $\frac{\pi}{4}$ Ans : (C)	$\frac{x}{a^2} + \frac{y}{b^2} = 1.$ TH extrix subtends (B) $\frac{x}{c}$	he portion of the tanger s at the corresponding f $\frac{\pi}{3}$	nt at a focus (C)	ny point of the curve int an angle of $\frac{\pi}{2}$	ercep (D)	ted between the point of $\frac{\pi}{6}$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direc (A) $\frac{\pi}{4}$ Ans : (C) Hint : Property	$\frac{x}{a^2} + \frac{y}{b^2} = 1. \text{ TI}$ strix subtends (B) $\frac{1}{2}$	he portion of the tanger s at the corresponding f $\frac{\pi}{3}$	nt at a focus (C)	ny point of the curve int an angle of $\frac{\pi}{2}$	ercep (D)	ted between the point of $\frac{\pi}{6}$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans : (C) Hint : Property A line cuts the x-axis a x-axis at P (a, 0) and	$\frac{x}{a^2} + \frac{y}{b^2} = 1. TI$ strix subtends (B) $\frac{1}{2}$ at A (7, 0) and I the y-axis at	he portion of the tanger s at the corresponding t $\frac{\pi}{3}$ d the y-axis at B (0, -5). t Q (0, b). If AQ and BF	nt at a focus (C) . A var P inter	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of	ercep (D) eerper R is	ted between the point of $\frac{\pi}{6}$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans: (C) Hint: Property A line cuts the x-axis at x-axis at P (a, 0) and (A) $x^2 + y^2 + 7x + 5$	$\frac{x}{a^2} + \frac{y}{b^2} = 1. \text{ TH}$ trix subtends (B) $\frac{1}{2}$ at A (7, 0) and the y-axis at y = 0 (B) x	he portion of the tanger s at the corresponding t $\frac{\pi}{3}$ d the y-axis at B (0, -5). t Q (0, b). If AQ and BF $x^2 + y^2 + 7x - 5y = 0$	nt at a focus (C) . A var P inter (C)	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of $x^2 + y^2 - 7x + 5y = 0$	ercep (D) perper R is (D)	ted between the point of $\frac{\pi}{6}$ indicular to AB cutting the $x^2 + y^2 - 7x - 5y = 0$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans: (C) Hint: Property A line cuts the x-axis at x-axis at P (a, 0) and (A) $x^2 + y^2 + 7x + 5$ Ans: (C)	$\frac{x}{a^2} + \frac{y}{b^2} = 1. \text{ TH}$ etrix subtends (B) $\frac{1}{2}$ at A (7, 0) and the y-axis at by = 0 (B) x	he portion of the tanger s at the corresponding t $\frac{\pi}{3}$ d the y-axis at B (0, -5). t Q (0, b). If AQ and BF $x^2 + y^2 + 7x - 5y = 0$	nt at a focus (C) . A var P inter (C)	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of $x^2 + y^2 - 7x + 5y = 0$	ercep (D) erper R is (D)	ted between the point of $\frac{\pi}{6}$ indicular to AB cutting the $x^2 + y^2 - 7x - 5y = 0$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans : (C) Hint : Property A line cuts the x-axis at x-axis at P (a, 0) and (A) $x^2 + y^2 + 7x + 5$ Ans : (C) Hint : P is orthocentre of $\Delta A$	$\frac{x}{a^2} + \frac{y}{b^2} = 1.$ The extrix subtends (B) $\frac{7}{2}$ at A (7, 0) and the y-axis at iy = 0 (B) x ABO	he portion of the tanger s at the corresponding the tanger $\frac{\pi}{3}$ d the y-axis at B (0, -5). t Q (0, b). If AQ and BF $x^2 + y^2 + 7x - 5y = 0$	nt at a focus (C) . A var P inter (C)	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of $x^2 + y^2 - 7x + 5y = 0$	ercep (D) erper R is (D)	$\frac{\pi}{6}$ ndicular to AB cutting the $x^{2} + y^{2} - 7x - 5y = 0$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans : (C) Hint : Property A line cuts the x-axis at x-axis at P (a, 0) and (A) $x^2 + y^2 + 7x + 5$ Ans : (C) Hint : P is orthocentre of $\Delta A$ m <sub>BR</sub> × m <sub>AR</sub> = -1	$\frac{x}{a^2} + \frac{y}{b^2} = 1. \text{ TI}$ trix subtends (B) $\frac{2}{3}$ at A (7, 0) and the y-axis at iy = 0 (B) x ABQ	he portion of the tanger is at the corresponding t $\frac{\pi}{3}$ d the y-axis at B (0, -5). t Q (0, b). If AQ and BF $x^2 + y^2 + 7x - 5y = 0$	nt at a focus (C) . A var P inter (C)	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of $x^2 + y^2 - 7x + 5y = 0$	ercep (D) eerper R is (D)	$\frac{\pi}{6}$ ndicular to AB cutting the $x^{2} + y^{2} - 7x - 5y = 0$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans : (C) Hint : Property A line cuts the x-axis at x-axis at P (a, 0) and (A) $x^2 + y^2 + 7x + 5$ Ans : (C) Hint : P is orthocentre of $\Delta A$ $m_{BR} \times m_{AR} = -1$ $\Rightarrow \left(\frac{k+5}{h}\right) \times \left(\frac{k}{h-7}\right) =$	$\frac{x}{a^2} + \frac{y}{b^2} = 1. \text{ Ti}$ ctrix subtends (B) $\frac{1}{2}$ at A (7, 0) and the y-axis at by = 0 (B) x ABQ = -1	he portion of the tanger is at the corresponding t $\frac{\pi}{3}$ d the y-axis at B (0, -5). It Q (0, b). If AQ and BF $x^2 + y^2 + 7x - 5y = 0$	nt at a focus (C) . A var P inter (C) ∖ 	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of $x^2 + y^2 - 7x + 5y = 0$	ercep (D) eerper R is (D)	$\frac{\pi}{6}$ indicular to AB cutting the $x^{2} + y^{2} - 7x - 5y = 0$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans : (C) Hint : Property A line cuts the x-axis at x-axis at P (a, 0) and (A) $x^2 + y^2 + 7x + 5$ Ans : (C) Hint : P is orthocentre of $\Delta A$ $m_{BR} \times m_{AR} = -1$ $\Rightarrow \left(\frac{k+5}{h}\right) \times \left(\frac{k}{h-7}\right) =$ $\Rightarrow x^2 + y^2 - 7x + 5y =$	$\frac{x}{a^2} + \frac{y}{b^2} = 1. \text{ Ti}$ ctrix subtends (B) $\frac{2}{3}$ at A (7, 0) and the y-axis at by = 0 (B) x ABQ = -1 = 0	he portion of the tanger is at the corresponding t $\frac{\pi}{3}$ d the y-axis at B (0, -5). It Q (0, b). If AQ and BF $x^2 + y^2 + 7x - 5y = 0$	A var (C) A var P inter (C)	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of $x^2 + y^2 - 7x + 5y = 0$	ercep (D) erper R is (D)	$\frac{\pi}{6}$ ndicular to AB cutting the $x^2 + y^2 - 7x - 5y = 0$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans : (C) Hint : Property A line cuts the x-axis at x-axis at P (a, 0) and (A) $x^2 + y^2 + 7x + 5$ Ans : (C) Hint : P is orthocentre of $\Delta A$ $m_{BR} \times m_{AR} = -1$ $\Rightarrow \left(\frac{k+5}{h}\right) \times \left(\frac{k}{h-7}\right) =$ $\Rightarrow x^2 + y^2 - 7x + 5y =$	$\frac{x}{a^2} + \frac{y}{b^2} = 1. \text{ Ti}$ ctrix subtends (B) $\frac{2}{3}$ at A (7, 0) and the y-axis at by = 0 (B) x ABQ = -1 = 0	he portion of the tanger is at the corresponding t $\frac{\pi}{3}$ d the y-axis at B (0, -5). It Q (0, b). If AQ and BF $x^2 + y^2 + 7x - 5y = 0$	A var (C) A var P inter (C)	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of $x^2 + y^2 - 7x + 5y = 0$	ercep (D) erper R is (D)	$\frac{\pi}{6}$ ndicular to AB cutting the $x^2 + y^2 - 7x - 5y = 0$	
60.	Consider the curve $\frac{\pi}{a}$ contact and the direct (A) $\frac{\pi}{4}$ Ans : (C) Hint : Property A line cuts the x-axis at x-axis at P (a, 0) and (A) $x^2 + y^2 + 7x + 5$ Ans : (C) Hint : P is orthocentre of $\Delta A$ $m_{BR} \times m_{AR} = -1$ $\Rightarrow \left(\frac{k+5}{h}\right) \times \left(\frac{k}{h-7}\right) =$ $\Rightarrow x^2 + y^2 - 7x + 5y =$	$\frac{x}{a^2} + \frac{y}{b^2} = 1. \text{ Ti}$ ctrix subtends (B) at A (7, 0) and the y-axis at by = 0 (B) x ABQ = -1 = 0	he portion of the tanger is at the corresponding t $\frac{\pi}{3}$ d the y-axis at B (0, -5). It Q (0, b). If AQ and BF $x^2 + y^2 + 7x - 5y = 0$	A var (C) A var (C)	ny point of the curve int an angle of $\frac{\pi}{2}$ riable line PQ is drawn p rsect at R, the locus of $x^2 + y^2 - 7x + 5y = 0$	ercep (D) erper R is (D)	$\frac{\pi}{6}$ ndicular to AB cutting the $x^2 + y^2 - 7x - 5y = 0$	

52. Let 
$$0 < \alpha < \beta < 1$$
. Then  $\lim_{n \to \infty} \sum_{k=1}^{n} \frac{(n+\alpha)}{1+\alpha} \frac{dx}{1+\alpha}$  is  
(A)  $\log_{n} \frac{\beta}{\alpha}$  (B)  $\log_{n} \frac{1+\beta}{1+\alpha}$  (C)  $\log_{n} \frac{1+\alpha}{1+\beta}$  (D)  $\infty$   
Ans: (B)  
Hin::  
 $\lim_{n \to \infty} \sum_{k=1}^{n} \left[\log(1+x) \frac{1}{k+\alpha}\right] -\log(1+\frac{1}{k+\beta}) \right]$   
 $=\lim_{n \to \infty} \sum_{k=1}^{n} \left[\log(1+\frac{1}{k+\alpha}) -\log(\frac{k+\beta+1}{k+\beta})\right]$   
 $=\log(\frac{\beta+1}{\alpha+1})$   
63.  $\lim_{n \to \infty} \left[\frac{1}{n} \left(\log(\frac{1}{k+\alpha}) - \log(\frac{k+\beta+1}{k+\beta})\right) -\log(\frac{k+\beta+1}{k+\beta})\right]$   
 $=\log(\frac{\beta+1}{n+1})$   
63.  $\lim_{n \to \infty} \left[\frac{1}{n} \left(\frac{1}{nx} - \frac{1}{x-1}\right) - \lim_{k=1} \frac{(x-1) - \ln x}{(x-1) \ln x} - \frac{1}{2}\right]$  (D) 0  
Ans: (C)  
Hint:  $\lim_{k \to 1} \left(\frac{1}{nx} - \frac{1}{x-1}\right) - \lim_{k \to 1} \frac{(x-1) - \ln x}{(x-1) \ln x} - \frac{1}{2}$   
Using L.H. rule twice  
64. Let  $y = \frac{4}{1+x+\ln x}$ . Then  
(A)  $x \frac{dy}{dx} + y = x$  (B)  $x \frac{dy}{dx} = y(y \ln x - 1)$  (C)  $x^{2} \frac{dy}{dx} = y^{2} + 1 - x^{2}$  (D)  $x \left(\frac{dy}{dx}\right)^{2} - y - x$   
Ans: (B)  
Hint:  $x \frac{dy}{dx} = y(y \ln x - 1)$ 

65. Consider the curve  $y = be^{-x/a}$  where a and b are non-zero real numbers. Then

(A) 
$$\frac{x}{a} + \frac{y}{b} = 1$$
 is tangent to the curve at (0, 0)

- (B)  $\frac{x}{a} + \frac{y}{b} = 1$  is tangent to the curve where the curve crosses the axis of y
- (C)  $\frac{x}{a} + \frac{Y}{b} = 1$  is tangent to the curve at (a, 0)
- (D)  $\frac{x}{a} + \frac{y}{b} = 1$  is tangent to the curve at (2a, 0)

Ans:(B)

**Hint**: 
$$y-b = -\frac{b}{a}(x) \Rightarrow \frac{x}{a} + \frac{y}{b} = 1$$

#### CATEGORY - III (Q66 to Q75)

Carry 2 marks each and one or more option(s) is/are correct. If all correct answers are not marked and no incorrect answer is marked then score = 2 × number of correct answers marked ÷ actual number of correct answers. If any wrong option is marked or if any combination including a wrong option is marked, the answer will considered wrong, but there is no negative marking for the same and zero marks will be awarded.

66. The area of the figure bounded by the parabola  $x = -2y^2$ ,  $x = 1 - 3y^2$  is

(A) 
$$\frac{1}{3}$$
 square unit  
(B)  $\frac{4}{3}$  square unit  
(C) 1 square unit  
(D) 2 square unit  
Ans: (B)  
Hint:  

$$A = \int_{-1}^{1} (1 - 3y^{2}) - (-2y^{2}) dy$$

$$\Rightarrow A = 2\int_{0}^{1} (1 - y^{2}) dy = \frac{4}{3}$$
(7)  
A particle is projected vertically upwards. If it has to stay above the ground for 12 seconds, then  
(A) velocity of projection is 192 ft/sec  
(B) greatest height attained is 600 ft  
(C) velocity of projection is 196 ft / sec  
(D) greatest height attained is 576 ft  
Ans: (A,D)  
Hint:  $V = u - gt$  at  $t = 6$   
 $u - gt = 0$   
 $\Rightarrow u = 6g = 192 ft / sec$   
 $(g = 32 ft / sec^{2}) \dots(i)$   
 $x = ut = \frac{1}{2} gt^{2}$   
 $= 192.6 - \frac{1}{2} 32.6^{2}$ 

WB.	JEE - 2020 (Answers & Hint)				Mathematics
	= 576ft				
68.	The equation $x^{(\log_3 x)^2 - \frac{9}{2}\log_3 x + 5} = 3\sqrt{3}$ has				
	(A) at least one real root	(B)	exactly one real root		
	(C) exactly one irrational root	(D)	complex roots		
	Ans: (A,C) Hint: $2t^3 + 10t + 3 = 0 + t = \log x$				
	1 = 100 = 3 = 0, t = 100 = 3				
	$\Rightarrow (t-3)(t-1)\left(t-\frac{1}{2}\right) = 0$				
<b>CO</b>	$\Rightarrow$ x = 3°,3',3'' <sup>2</sup>	الم م ا		a at 1	
69.	= 1, 2, n. If the total number of wrong answers given	is 20	947, then n is equal to	oati	east i questions, where i
	(A) 10 (B) 11	(C)	12	(D)	13
	Ans : (B) Hint : Total students was dave wrong answer to exactly	i – a	uestions - $2^{n-i} - 2^{n-(i+1)}$		
	Total wrong answer given = $\sum i \times (2^{n-i} - 2^{n-(i+1)})$	Ч			
	$\Rightarrow 2^{n-1} + \dots 1 = 2047$				
	$\Rightarrow 2^{n} = 2048$				
	$\Rightarrow$ n = 11		1		
70.	A and B are independent events. The probability that both a occurs is $\frac{3}{5}$ . The probability of occurrence of A is	Aand	Boccur is $\frac{1}{20}$ and the p	oroba	bility that neither of them
	(A) $\frac{1}{2}$ (B) $\frac{1}{10}$	(C)	$\frac{1}{4}$	(D)	<u>1</u> 5
	Ans : (C,D)				
	$Hint: P(A' \cap B') = \frac{3}{5}$				
	$\Rightarrow 1 - P(A \cup B) = \frac{3}{5}$				
	$\Rightarrow P(A \cup B) = \frac{2}{5}$				
	$\Rightarrow P(A) + P(B) - P(A).P(B) = \frac{2}{5}$				
	$\Rightarrow P(A) + P(B) = \frac{9}{20}$ and $P(A).P(B) = \frac{1}{20}$				
71.	The equation of the straight line passing through the point sum is $-1$ is	(4, 3)	and making intercepts of	on the	e co-ordinate axes whose
	(A) $\frac{x}{2} - \frac{y}{3} = 1$ (B) $\frac{x}{-2} + \frac{y}{1} = 1$	(C)	$-\frac{x}{3}+\frac{y}{2}=1$	(D)	$\frac{x}{1} - \frac{y}{2} = 1$
	Ans : (A,B)				

Hint : Let line be 
$$\frac{x}{a} + \frac{y}{b} = 1$$
, then  $a+b = -1$   
 $\frac{4}{a} - \frac{3}{1+a} = 1 \Rightarrow a = \pm 2$   
72. Consider a tangent to the ellipse  $\frac{x^2}{2} + \frac{y^2}{1} = 1$  at any point. The locus of the midpoint of the portion intercepted between the axes is  
(A)  $\frac{x^2}{2} + \frac{x^2}{4} = 1$  (B)  $\frac{x^2}{4} + \frac{y^2}{2} = 1$  (C)  $\frac{1}{3x^2} + \frac{1}{4y^2} = 1$  (D)  $\frac{1}{2x^2} + \frac{1}{4y^2} = 1$   
Ans : (D)  
Hint : Tangent at P(x, y.)  
 $\frac{xx}{2} + \frac{yy}{1} = 1$   
Let mid point of intercept be P(h, k)  
 $h = \frac{1}{x}, k = \frac{1}{2y_1}$  or  $x_1 = \frac{1}{h}, y_1 = \frac{1}{2k}$   
locus is  $\frac{1}{2x^2} + \frac{4y}{4y^2} = 1$   
73. Let  $y = \frac{x^2}{(x+1)^2(x+2)}$ . Then  $\frac{d^2y}{dx^2}$  is  
(A)  $2\left[\frac{3}{(x+1)^2} - \frac{3}{(x+1)^2} + \frac{4}{(x+2)^3}\right]$  (D)  $\frac{7}{(x+1)^2} - \frac{3}{(x+1)^2} + \frac{3}{(x+1)^2}$   
(D)  $\frac{7}{(x+1)^2} - \frac{3}{(x+1)^2} + \frac{2}{(x+1)^2}$   
Ans : (A)  
Hint : By partial fraction technique  
 $y = \frac{x^2}{(x+1)^2(x+2)} = \frac{4}{(x+2)} - \frac{3}{(x+1)} + \frac{1}{(x+1)^2}$   
 $\Rightarrow y' = \frac{6}{(x+1)^3} - \frac{6}{(x+1)^3} + \frac{8}{(x+2)^3}$ 



Answer Keys by				
	Aaka	sh Institute,	Kolkata Centre	
Q.No.	\$			
01	В	C	C	C
02	B	A	В	C
04	С	D	А	A
05	A	A	A	В
06	D	<u> </u>	В	D
08	D	C	B	C
09	В	В	С	В
10	A	А	A	A
11	A	A	D	D
12	A C	D	D	A
14	В	В	В	C
15	С	С	A	С
16	A	A	A	В
17	В	<u>D</u>	A	A A
19	A	D	В	B
20	C	B	C	D
21	В	А	A	В
22	A	A	В	С
23	D	A	D	A
24	A	R	A C	D
26	C	C	В	D
27	C	A	A	В
28	В	В	D	A
29	A	D	Α	A
30	A	A	D	A
32	B	B	C B	A C
33	A	C	В	В
34	С	B	A	C
35	В	A	C	В
36	В	D	A,C,D	A
37	D	A,C,D	B	D
39	D	D	A	A,C,D B
40	A,C,D	A	D	D
41	С	В	A	A
42	C	В	С	В
43	В	C	D	B
4-4 45	C	A	C C	A
46	Ă	C	В	C
47	D	D	D	С
48	В	С	С	A
49	A	C	A	D
51	R	<u>в</u>	R	A
52	B	C	A	A
53	D	A	A	D
54	A	D	В	D
55	C	B	B	B
50	Δ	Δ	Δ	с В
58	D	B	C	c
59	A	В	C	A
60	С	D	A	С
61	A	A	D	D
62 63	D	C	A	C
64	B	C	A	B
65	В	D	D	D
66	С	A	D	C
67	С	С	В	A
68	A	A	B	D
70		<u>ט</u>		В
71	D	C C	D	
72	В	D	D	C
73	D	D	В	D
74	С	В	D	D
75	D	D	C	B
76	A,B	A,C,D	A,C	A,B,D
78	л, в, D A.B.D	A,C A R	A,D A,B D	A,C,D
79	A,C,D	A,B,D	A,B,D	A.B
	1.0		ACD	



**Physics & Chemistry** 





**ANSWERS & HINT** 

## for

## WBJEE - 2020 SUB : PHYSICS & CHEMISTRY

## PHYSICS

## CATEGORY - I (Q1 to Q30)

Carry 1 mark each and only one option is correct. In case of incorrect answer or any combination of more than one answer, <sup>1</sup>/<sub>4</sub> mark will be deducted.

1. The intensity of light emerging from one of the slits in a Young's double slit experiment is found to be 1.5 limes the intensity of light emerging from the other slit. What will be the approximate ratio of intensity of an interference maximum to that of an interference

(A) 2.25	(B) 98	(C) 5	(D) 9.9
----------	--------	-------	---------

Ans : (B)

**Hint :**  $I_1 = 1.5I_2$ 

$$\frac{I_1}{I_2} = \frac{3}{2} \cdot \frac{I_{max}}{I_{min}} = \left(\frac{\sqrt{I_1} + \sqrt{I_2}}{\sqrt{I_1} - \sqrt{I_2}}\right)^2 = \left(\frac{\sqrt{3} + \sqrt{2}}{\sqrt{3} - \sqrt{2}}\right)^2 = 98$$

- 2. In a Frounhofer diffraction experiment, a single slit of width 0.5 mm is illuminated by a monochromatic light of wavelength 600 nm. The diffraction pattern is observed on a screen at a distance of 50 cm from the slit. What will be the linear separation of the first order minima ?
  - (A) 1.0 nm (B) 1.1 nm (C) 0.6 mm (D) 1.2 nm

Ans:(D)

Hint : d=0.5 mm.

 $\lambda$ =600 nm. Width of central maxima =  $\frac{2\lambda D}{d}$ 

D = 50 cm

$$\frac{2\lambda D}{d} = \frac{2 \times 600 \times 50 \times 10^{-2} \times 10^{-9}}{0.5 \times 10^{-3}} = 1.2 \text{mm}$$

## 3. If R is the Rydberg Constant in cm<sup>-1</sup>, then hydrogen atom does not emit any radiation of wave-length in the range of

(A) 
$$\frac{1}{R}$$
 to  $\frac{4}{3R}$  cm (B)  $\frac{7}{5R}$  to  $\frac{19}{5R}$  cm (C)  $\frac{4}{R}$  to  $\frac{36}{5R}$  cm (D)  $\frac{9}{R}$  to  $\frac{144}{7R}$  cm

Ans: (B)  
Hint: 
$$\frac{1}{\lambda} = R \left[ \frac{1}{n_c} - \frac{1}{n_c} \right]$$
  
For range of wavelengths:  
 $n = 1, 2, 3, ..., for Lyman, Balmer, Paschen, ...., n, n + 1 and n = x for upper and lower range
Thus, Lyman:  $\left[ \frac{1}{R} \ln \frac{4}{3R} \right]$ , Balmer:  $\left[ \frac{4}{R} \ln \frac{36}{5R} \right]$ , Paschen:  $\left[ \frac{9}{R} \ln \frac{144}{3RR} \right]$ , Bracket:  $\left[ \frac{15}{R} \ln \frac{400}{9R} \right]$ , Pfund:  $\left[ \frac{25}{R} \ln \frac{500}{11R} \right]$   
4. A nucleus X emits a beta particle to produce a nucleus Y. If their atomic masses are M, and M, respectively, the maximum energy of the beta particle emitted is (where m, is the mass of an electron and c is the velocity of light)  
(A)  $(M_1 - M_2 - m_3)c^2$  (B)  $(M_2 - M_2 + m_3)c^2$  (C)  $(M_4 - M_2)c^2$  (D)  $(M_4 - M_2 - 2m_3)c^2$   
Ans: (C)  
 $m_1 - M_4 - 2m_4$   
Hint:  $\frac{1}{2}X^4 \rightarrow \frac{2}{N_1 + e^2} + \overline{v} + Q$   
 $m_1 - M_2 - 2m_4$   
 $R - M_1 - M_2 + m_4$   
 $E - \Delta mc^2 = (m_1 - m_2 - m_3)C^2 = (M_1 - M_3)C^2$   
5. For nuclei with mass number close to 119 and 238, the binding energies per nucleon are approximately 7.6 MeV and 8.6 MeV respectively. If a nucleus of mass number 238 breaks into two nuclei of nearly equal masses, what will be the approximate amount of energy released in the process of fission ?  
(A) 214 MeV (B) 119 MeV (C) 2047 MeV (D) 1142 MeV  
Ans: (A)  
Hint: 119  $\rightarrow 7.6 MeV$   
238  $\rightarrow 8.8 MeV$   
238  $\rightarrow 119 + 119$   
 $E_{-230 + 7.6}$   
 $E_{-230 + 7.6}$   
(A) 30 (B) 640 (C) 900 (D) 720  
Ans: (D)  
Hint:  $R_{c} = 6 \times 10^{10}$$ 

Physics & Chemistry

WBJEE - 2020 (Answers & Hint)

## **Physics & Chemistry**

## WBJEE - 2020 (Answers & Hint)

$$\begin{aligned} \Delta l_{q} R_{q} &= 15 \times 10^{-3} V \\ \Delta l_{g} &= 20 \times 10^{-8} A \\ A_{v} &= 1.8 \times 10^{-3} A \\ A_{v} &= \beta_{v} \frac{R_{v}}{R_{v}} &= \frac{A_{v}}{A_{v}}, \frac{R_{v}}{R_{v}} &= \frac{18 \times 10^{-5}}{20 \times 10^{-5}} \times \frac{6 \times 10^{+5} \times 20 \times 10^{-6}}{15 \times 10^{-5}} = 720 \end{aligned}$$
In the circuit shown, the value of  $\beta$  of the transistor is 48. If the base current supplied is 200 µA, what is the voltage at the terminal Y?
$$(A) \quad 0.2V \qquad (B) \quad 0.5V \qquad (C) \quad 4V \qquad (D) \quad 4.8V \\ Ans: (A) \\ Hint: \beta &= 48 \\ l_{v} &= 200\mu A \\ l_{v} &= \beta l_{v} = 48 \times 200 \times 10^{-6} \\ V_{C0} &= l_{v} R_{v} + V_{c1} + V_{c1} = 5 - (96 \times 10^{-1}) \times 500 = 5 - 4.8 = 0.2 \text{ volt} \end{aligned}$$
8. The frequency v of the radiation emitted by an atom when an electron jumps from one orbit to another is given by v = k \delta E, where k is a constant and  $\delta E$  is the change in energy level due to the transition. Then dimension of k is 
$$(A) \quad ML^{T-1} \qquad (B) \quad \text{the same dimension of angular momentum} \\ (C) \quad ML^{T-1} \qquad (D) \quad M^{-1}L^{-T} \\ Ans: (D) \\ Hint: v = k\delta E \\ [k] = \left[\frac{V}{\delta E}\right] = \frac{[T^{-1}]}{[ML^{T-1}]} \\ [k] = [M^{-1}L^{-1}T] \\ 9. \quad Consider the vectors \ \overline{A} = \overline{i} + \overline{j} \cdot \overline{k}, \ \overline{B} = 2\overline{i} - \overline{j} + \overline{k}, \ \overline{C} = \frac{1}{\sqrt{5}} (\overline{i} - 2\overline{j} + 2\overline{k}). What is the value of \ \overline{C}_{v}(\overline{A} \times \overline{B})? \\ (A) \quad 1 \qquad (B) \quad 0 \qquad (C) \quad 3\sqrt{2} \qquad (D) \quad 18\sqrt{5} \\ Ans: (B) \end{aligned}$$

Hint: 
$$\vec{C} \cdot (\vec{A} \times \vec{B}) = \begin{vmatrix} 1 & 1 & -1 \\ 2 & -1 & 1 \\ 1 & -2 & 2 \end{vmatrix} = 1(-2+2) - 1(4-1) - 1(-4+1) = -3+3 = 0$$

- 10. A fighter plane, flying horizontally with a speed 360 kmph at an altitude of 500 m drops a bomb for a target straight ahead of it on the ground. The bomb .should be dropped at what approximate distance ahead of the target ? Assume that acceleration due to gravity (g) is 10 ms<sup>-2</sup>. Also neglect air drag
  - (A) 1000 m (B)  $50\sqrt{5}$  m (C)  $500\sqrt{5}$  m (D) 866 m

Ans:(A)

**Hint :** v = 360 km/h = 100 m/s.

h=500 m

$$R = u \sqrt{\frac{2h}{g}} = 100 \times \sqrt{\frac{2 \times 500}{10}} = 1000m$$

11. A block of mass m rests on a horizontal table with a co-efficient of static friction μ. What minimum force must be applied on the block to drag it on the table ?

(A) 
$$\frac{\mu}{\sqrt{1+\mu^2}}$$
 mg (B)  $\frac{\mu-1}{\mu+1}$  mg (C)  $\frac{\mu}{\sqrt{1-\mu^2}}$  mg (D)  $\mu$ mg  
Ans: (C)  
Hint: Fsine N of F of Fcose  
F sine + N = mg N = mg - F sine  
F cose =  $\mu$ (mg - F sine)  $F = \frac{\mu}{\cos \theta + \mu} \sin \theta$ ,  
for F<sub>man</sub>,  $\frac{d}{d\theta} [\cos \theta + \mu \sin \theta] = 0$   
 $\therefore$  tan  $\theta = \mu$   
 $\therefore \frac{F_{man} = \frac{\mu}{\sqrt{1+\mu^2}}}{1}$   
12. A tennis ball hits the floor with a speed v at an angle  $\theta$  with the normal to the floor. If the collision is inelastic and the co-efficient of restitution is  $\varepsilon$ , what will be the angle of reflection ?  
(A)  $\tan^{-1} \left(\frac{\tan \theta}{\varepsilon}\right)$  (B)  $\sin^{-1} \left(\frac{\sin \theta}{\varepsilon}\right)$  (C)  $\theta\varepsilon$  (D)  $\theta \frac{2\varepsilon}{\varepsilon+1}$   
Ans: (A)









21. A very long charged solid cylinder of radius 'a' contains a uniform charge density ρ. Dielectric constant of the material of the cylinder is k. What will be the magnitude of electric field at a radial distance 'x' (x < a) from the axis of the cylinder ?</p>

(A) 
$$p_{R_{0}}^{X}$$
 (B)  $p_{2R_{0}}^{X}$  (C)  $p_{2R_{0}}^{X^{2}}$  (D)  $p_{\frac{X^{2}}{2K}}^{X}$   
Ans : (B)  
Hint : Using Gauss's Law  
 $E(2\pi \kappa)_{g} = \frac{p(\pi \chi^{2})}{k_{e_{0}}}$  :  $E = \frac{p\chi}{2k_{e_{0}}}$   
22. A galvanometer can be converted to a voltmeter of full-scale deflection V<sub>0</sub> by connecting a series resistance R, and can be converted to an ammeter of full-scale deflection V<sub>0</sub> by connecting a series resistance R, and can be converted to an ammeter of full-scale deflection ?  
(A)  $\frac{V_{1}-UR_{1}}{R_{1}-R_{2}}$  (B)  $\frac{V_{2}+UR_{1}}{R_{1}+R_{2}}$  (C)  $\frac{V_{1}-UR_{2}}{R_{2}-R_{1}}$  (D)  $\frac{V_{1}+UR_{2}}{R_{1}+R_{2}}$   
Ans : (A)  
Hint : R,  $=\frac{V_{0}}{V_{0}} = G$ ......(1)  
 $R_{2} = \frac{V_{0}-UR_{2}}{U_{1}-U_{1}}$  (D)  $\frac{W_{1}+UR_{2}}{R_{1}+R_{2}}$   
As shown in the figure, a single conducting wire is bent to form a loop in the form of a circle of radius Y concentrically inside a square of side 'a', where a : r = 8 : r. A battery B drives a current through the wire. If the battery B and the gap G are of negligible sizes, determine the strength of magnetic field at the common centre O.  
(A)  $\frac{U_{1}-UR_{2}}{2\pi a}\sqrt{2}(\sqrt{2}-1)$  (B)  $\frac{U_{2}}{2\pi a}(\sqrt{2}+1)$  (C)  $\frac{H_{2}}{\pi a}2\sqrt{2}(\sqrt{2}+1)$  (D)  $\frac{H_{2}}{\pi a}2\sqrt{2}(\sqrt{2}-1)$   
Ans : (D)  
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**Hint :**  $\frac{a}{r} = \frac{8}{\pi}$ ,  $r = \frac{\pi a}{8}$ 



$$B = \frac{\mu_0 l}{2r} - \frac{4\mu_0 l}{4\pi^2 2} \times \sqrt{2} = \frac{\mu_0 l}{2r} - \frac{2\sqrt{2}\mu_0 l}{\pi a} = \frac{\mu_0 l \times 8}{2\pi a} - \frac{2\sqrt{2}\mu_0 l}{\pi a}$$
$$= \frac{\mu_0 l}{\pi a} (4 - 2\sqrt{2}) = \frac{\mu_0 l}{\pi a} 2\sqrt{2} (\sqrt{2} - 1)$$
$$X = \frac{X \times X \times X}{X \times X} \times \frac{X \times X}{X \times X} \times \frac{X}{X \times X} \times \frac{X}{X} \times \frac{X}{X \times X} \times \frac{X}{X \times X} \times \frac{X}{X} \times \frac{X}{X} \times \frac{X}{X} \times \frac{X}{X} \times \frac{X}{X} \times \frac{X}{$$

As shown in the figure, a wire is bent to form a D-shaped loop, carrying current I, where the curved part is semi-circle of radius R. the loop is placed in a uniform magnetic field B, which is directed into the plane of the paper. The magnetic force left by the closed loop is

(A)	0	(B)	IRB	(C)	2IRB	(D)	$\frac{1}{2}$ IRB
							2

## Ans:(A)

Hint : Zero (Net magnetic force on a closed current loop in a uniform  $\vec{B}$  is zero)



What will be the equivalent resistance between the terminals A and B of the infinite resistive network shown in the figure?







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$$\tan\theta = \frac{v_y}{v_x} = \frac{evL}{mdv_0.v_0}$$

$$\Rightarrow \ \theta = tan^{-1} \left( \frac{evL}{mdv_0^2} \right)$$

33. A metallic block of mass 20 kg is dragged with a uniform velocity of 0.5 ms<sup>-1</sup> on a horizontal table for 2.1s. The co-efficient of static friction between the block and the table is 0.10. What will be the maximum possible rise in temperature of the metal block if the specific heat of the block is 0.1 C.G.S unit ? Assume g=10 ms<sup>-2</sup> uniform rise in temperature throughout the whole block. [Ignore absorption of heat by the table]

(A) 0.0025 °C (B) 0.025 °C (C) 0.001 °C (D) 0.05 °C  
Ans: (B)  
Hint: friction f = 
$$\mu$$
 mg = 0.1×20×10 = 20  
W, = heat  
 $\Rightarrow (f.u)t = mc \Delta T$   
 $\Rightarrow 20x0.5x2.1 = 20x0.1x4.2x10°. \Delta T$   
 $\Rightarrow \Delta T = 0.0025 °C$   
3. Consider an engine that absorbs 130 cal of heat from a hot reservoir and delivers 30 cal heat to a cold reservoir in each  
cycle. The engine also consumes 2.1 energy in each cycle to vercome friction. If the engine works at 90 cycles per  
minute, what will be the maximum power delivered to the load ? [Assume the thermal equivalent of heat is 4.2J/cal]  
(A) 816 W (B) 819 W (C) 627 W (D) 630 W  
Ans: (C)  
Hint: work done per cycle = 100×4.2-2 = 418J  
Total work done per cycle = 100×4.2-2 = 418J  
Total work done per cycle = 100×4.2-2 = 418J  
Total work done per cycle = 100×4.2-2 = 418J  
Total work done = 418 × 90  
Power =  $\frac{418 \times 90}{60} = 627 W$   
35. Two pith balls, each carrying charge +q are hung from a hook by two strings. It is found that when each charge is  
tripled, angle between the strings double. What was the initial angle between the strings ?  
(A) 30° (B) 60° (C) 45° (D) 90°  
Ans: (B)  
Hint : T sin0 = Fe, T cos0 = mg  
 $\tan \theta = \frac{Fe}{mg} = \frac{kq^2}{(2L \sin \theta)^2 \cdot mg}$   
 $\ln 2nd case
 $\tan 2\theta = \frac{kq^2}{(2L \sin \theta)^2 \cdot mg}$   
 $\ln 2nd case
 $\tan 2\theta = \frac{9 \sin^2 \theta}{(2L \sin \theta)^2 \cdot mg}$   
 $\ln 2nd case
 $\tan 2\theta = \frac{9 \sin^2 \theta}{(2L \sin \theta)^2 \cdot mg}$   
 $\ln 2nd case - \frac{1}{1 - \tan^2 \theta} = \frac{9 \sin^2 \theta}{4(1 - \tan^2 \theta)}$$$$ 

~

$$\tan^2\theta = x, \quad \frac{2}{1-x} = \frac{9}{4}(1+x)$$

$$\Rightarrow 8 = 9 - 9x^2 \Rightarrow x = \frac{1}{3} \Rightarrow \tan^2 \theta = \frac{1}{3} \Rightarrow \theta = 30^\circ$$

Angle between the strings =  $2\theta$  =  $60^{\circ}$ 

## Category III (Q36 to Q40)

Carry 2 marks each and one or more option (s) is/are correct. If all correct answers are not marked and also no incorrect answer is marked then score =  $2 \times \text{number}$  of correct answers marked  $\div$  actual number of correct answers. If any wrong option is marked or if any combination including a wrong option is marked, the answer will be considered wrong, but there is no negative marking for the same and zero mark will be awarded.

- 36. A point source of light is used in an experiment of photo-electric effects. If the distance between the source and the photo-electric surface is doubled, which of the following may result ?
  - (A) Stopping potential will be halved
  - (B) photo-electric current will decrease
  - (C) Maximum kinetic energy if photo-electrons will decrease
  - (D) Stopping potential will increase slightly

Ans:(B)

**Hint** : Intensity  $I \propto \frac{1}{r^2}$ 

and photo-electric current  $\, \propto \,$  intensity

- ... Current will decrease
- 37. Two metallic spheres of equal outer radii are found to have same moment of inertia about their respective diameters. Then which of the following statement(s) is/are true ?
  - (A) The two spheres have equal masses
  - (B) The ratio of their masses is nearly 1.67 : 1
  - (C) The spheres are made of different materials
  - (D) Their rotational kinetic energies will be equal when rotated with equal uniform angular speed about their respective diameters

## Ans : (D)

~

Hint: Inner radius is not given

- $\therefore$  only option (D) is correct
- 38. A simple pendulum of length  $\ell$  is displaced so that its taught string is horizontal and then released. A uniform bar pivoted at one end is simultaneously released from its horizontal position. If their motions are synchronous, what is the length of the bar ?

(A) 
$$\frac{3\ell}{2}$$
 (B)  $\ell$  (C)  $2\ell$  (D)  $\frac{2\ell}{3}$   
Ans: (A)  
Hint:  $v = \sqrt{2gh}$   
 $= \sqrt{2gl\sin\theta}$ 

## Physics & Chemistry







Ans:(A)

Hint: It's perkin reaction. The reaction starts with generation of nucleophile from propanoic anhydride as follows :



Then onwards, the nucleophile attacks the -CHO group as shown :



Finally, it goes on to give :



WB.	EE - 2020 (Answers & Hint)					Physics & Chemistry
47.	The maximum number of elec and $m = -1$ is	trons in an atom in which th	ne las	t electron filled has the	quan	tum numbers n = 3, l = 2
	(A) 17 (B)	27	(C)	28	(D)	30
	Ans : (D)					
	<b>Hint :</b> n = 3 and I = 2 means 30 to any one. For maximum num	J-orbital. Since five orienta ber of electrons as asked,	tions answ	of d-orbitals are degen /er should be atomic nt	erate, umber	m = -1 can be assigned 30.
48.	In the face-centred cubic lattic length of the cubic unit cell)	ce structure of gold the clo	osest	distance between gold	1 atom	ns is ('a' being the edge
	(A) <sub>a√2</sub> (B)	$\frac{a}{\sqrt{2}}$	(C)	$\frac{a}{2\sqrt{2}}$	(D)	2√2a
	Ans : (B)					
	Hint: Closest distance betwee	en two gold atoms in fcc lat	ttice c	of gold is $rac{a}{\sqrt{2}}$ . This is the	e dista	ance between the corner
	atom and the closest face cent	tre atom.				
49.	The equilibrium constant for the	e following reactions are giv	ven af	t 25°C		
	$2A \rightleftharpoons B + C, K_1 = 1.0$					
	$2B \rightleftharpoons C + D, K_2 = 16$					
	$2C + D \rightleftharpoons 2P, K_3 = 25$					
	The equilibrium constant for th	the reaction $P \rightleftharpoons A + \frac{1}{2}B$ at	t 25°C	Cis		
	(A) $\frac{1}{20}$ (B)	20	(C)	<u>1</u> 42	(D)	21
	Ans:(A)					
	Hint: We can manipulate the	given equations as follows	;			
	$\frac{1}{2}B + \frac{1}{2}C \rightleftharpoons A, \qquad K'_1 = 1$					
	$\frac{1}{2}C + \frac{1}{2}D \rightleftharpoons B, \qquad \qquad K'_2 = \frac{1}{\sqrt{16}}$					
	$P \rightleftharpoons C + \frac{1}{2}D, \qquad \qquad K'_3 = \frac{1}{\sqrt{25}}$					
	$P \rightleftharpoons A + \frac{1}{2}B, \qquad K_{\text{final}} = 1 \times$	$\frac{1}{4} \times \frac{1}{5} = \frac{1}{20}$				
50.	Among the following, the ion w	hich will be more effective	for flc	occulation of Fe(OH), se	ol. is	
	(A) PO <sup>3-</sup> (B)	SO <sub>4</sub> <sup>2-</sup>	(C)	SO <sub>2</sub> <sup>2-</sup>	(D)	NO <sub>2</sub> -
	Ans:(A)	4	. ,	3		3
	<b>Hint</b> : $Fe(OH)_3$ is a positive so	I. PO <sub>4</sub> <sup>3-</sup> carrying the highes	st –ve	charge amongst the gi	iven ic	ons is most effective
51.	The mole fraction of ethanol ir	water is 0.08. Its molality i	is			
	(A) 6.32 mol kg <sup>-1</sup> (B) Ans : (B)	4.83 mol kg <sup>-1</sup>	(C)	3.82 mol kg <sup>-1</sup>	(D)	2.84 mol kg <sup>-1</sup>

Hint : Molality =  $\frac{x_{EtOH}}{x_{H_2O}} \times \frac{1000}{MW_{solvent}}$  $=\frac{0.08}{0.92} imes \frac{1000}{18}$  $= 4.83 \text{ mol kg}^{-1}$ 52. 5 ml of 0.1 M Pb(NO<sub>3</sub>), is mixed with 10 ml of 0.02 M Kl. The amount of Pbl, precipitated will be about (C) 2× 10<sup>-4</sup> mol (A) 10<sup>-2</sup> mol (B) 10<sup>-4</sup> mol (D) 10<sup>-3</sup> mol Ans:(B)  $\mathsf{Pb}\big(\mathsf{NO}_3\big)_{\!\!\!\!2} \ \ \text{(aq.)} \ + 2\mathsf{KI}\,(\mathsf{aq.}) \ \longrightarrow \ \ \mathsf{PbI}_2 \ \downarrow \ + 2\mathsf{KNO}_3 \ \ (\mathsf{aq.})$ 0 10×0.02 **Hint :** Initial milimole  $5 \times 0.1$ = 0.5 = 0.2 Final milimole 0.1 0 0.1 0.2 mole of Pbl<sub>2</sub> PPt =  $\frac{0.1}{1000} = 1 \times 10^{-4}$ 53. At 273 K temperature and 76 cm Hg pressure, the density of a gas is 1.964gL<sup>-1</sup>. The gas is (A) CH (B) CO (D)  $CO_2$ (C) He Ans:(D) Hint : Molar mass of gas (M) =  $\frac{dRT}{P} = \frac{1.964 \times 0.0821 \times 273}{1}$ = 44gHence, the gas is CO<sub>2</sub> 54. Equal masses of ethane and hydrogen are mixed in a empty container at 298 K. The fraction of total pressure exerted by hydrogen is (A) 15:16 (B) 1:1 (C) 1:4 (D) 1:6 Ans:(A) Hint : Let mass of ethane and H<sub>2</sub> are x g.  $n_{H_2} = \frac{x}{2}$  and  $n_{C_2H_6} = \frac{x}{30}$  $\frac{P_{H_2}}{P_T} = \frac{n_{H_2}}{n_{H_2} + n_{C_2H_6}} = \frac{\frac{x}{2}}{\frac{x}{2} + \frac{x}{20}} = \frac{15}{16}$ 55. An ideal gas expands adiabatically against vaccum. Which of the following is correct for the given process? (A)  $\Delta S = 0$ (B)  $\Delta T = -ve$ (C)  $\Delta U = 0$ (D)  $\Delta P = 0$ Ans:(C) Hint : For adiabatic free expansion of an ideal gas dq = 0dU = 0dH = 0dT = 0Aakash Educational Services Limited - Regd. Office: Aakash Tower, 8, Pusa Road, New Delhi-110005, Ph.: 011-47623456

WBJ	JEE - 2020 (Answers & Hint)				Physics & Chemistry
56.	$K_{f}$ (water) = 1.86 K kg mol <sup>-1</sup> . The temperature at which ic glycol is	e beg	ins to separate from a m	nixtur	e of 10 mass % ethylene
	(A) -1.86 °C (B) -3.72 °C	(C)	– 3.3 °C	(D)	−3 °C
	Ans : (C)				
	<b>Hint :</b> $\Delta T_f = K_f \times m$				
	$=1.86\left(\frac{10}{62}\times\frac{1000}{90}\right)$				
	= 3.3°C				
	$\therefore$ Temparature at which ice begins to separate = 3.3°C				
57.	The radius of the first Bohr orbit of a hydrogen atom is 0.5 is	3 × 10	r <sup>®</sup> cm. The velocity of the	e elec	tron in the first Bohr orbit
	(A) $2.188 \times 10^8 \text{ cm s}^{-1}$ (B) $4.376 \times 10^8 \text{ cm s}^{-1}$	(C)	1.094 × 10 <sup>8</sup> cm s⁻¹	(D)	2.188 × 10 <sup>9</sup> cm s <sup>-1</sup>
	Ans : (A)				
	Hint : $r = 0.53 \times 10^{-8} \text{ cm} = 0.53 \times 10^{-8} \text{ n}^2$				
	∴ n = 1				
	$V = 2.18 \times 10^8 \text{ cm/s}$				
58.	Which of the following statements is not true for the read	ction	$2F_2 + 2H_2O \rightarrow 4HF + O_2$	?	
	(A) $F_2$ is more strongly oxidising than $O_2$	(B)	F – F bond is weaker t	han (	D = O bond
	(C) $H - F$ bond is stronger than $H - O$ bond	(D)	F is less electronegative	ve tha	an O
	Ans : (D)				
	Hint : F is more electronegative than O				
59.	The number of unpaired electrons in the uranium ( $_{_{92}}$ U) at	om is			
	(A) 4 (B) 6	(C)	3	(D)	1
	Ans : (A)				
	Hint: $_{92}$ U : $[R_n]^{86}$ 5f <sup>3</sup> 6d <sup>1</sup> 7s <sup>2</sup>				
60.	How and why does the density of liquid water change on	prolo	nged electrolysis?		
	(A) Decreases, as the proportion of $H_2O$ increases	(B)	Remains unchanged		
	(C) Increases, as the proportion of $D_2O$ increases	(D)	Increases, as the volu	me de	ecreases
	Ans : (C)				
	Hint : $H_2O$ decomposes preferentially. Consequently $D_2O$	) con	centration increases an	d den	sity increases.
61.	The difference between orbital angular momentum of an	elect	ron in a 4f orbital and an	other	electron in a 4s orbital is
	(A) $2\sqrt{3}$ (B) $3\sqrt{2}$	(C)	$\sqrt{3}$	(D)	2
	Ans : (A)				
	<b>Hint</b> : Orbital angular momentum = $\sqrt{\ell(\ell+1)} \frac{h}{m}$				
	$\sqrt{\sqrt{2\pi}}$				



**Physics & Chemistry** 



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